```
List comprehensions:
                                                                                                                                                                                List & dictionary mutation:
  Numeric types in Python:
                                  Represents
                                                                           [<map exp> for <name> in <iter exp> if <filter exp>]
                                                                                                                                                                                >>> a = [10]
  >>> type(2)
                                                                                                                                                                                                               >>> b = [10]
                                                                                                                                                                               >>> b = a
  <class 'int'>.
                              integers exactly
                                                                            Short version: [<map exp> for <name> in <iter exp>]
                                                                                                                                                                               >>> a == b
                                                                                                                                                                                                               >>> a == b
  >>> type(1.5)
                               Represents real
                                                                                                                                                                                                               True
                                                                                                                                                                               True
                                                                       A combined expression that evaluates to a list using this
  <class 'float'><
                                 numbers with
                                                                                                                                                                               >>> a.append(20)
                                                                                                                                                                                                               >>> b.append(20)
                                                                       evaluation procedure:
                             finite precision
                                                                                                                                                                               >>> a == b
                                                                                                                                                                                                               >>> a
                                                                       1. Add a new frame with the current frame as its parent
                                                                                                                                                                               True
                                                                                                                                                                                                               [10]
 Rational implementation using functions:
                                                                       2. Create an empty result list that is the value of the
                                                                                                                                                                               >>> a
                                                                                                                                                                                                               >>> b
                                                                           expression
                                                                                                                                                                               [10, 20]
                                                                                                                                                                                                               [10, 20]
 def rational(n, d):
                                                                       3. For each element in the iterable value of <iter exp>:
                                                                                                                                                                                >> b
                                                                                                                                                                                                                >>> a == b
        def select(name):
                                                                          A. Bind <name> to that element in the new frame from step 1
                                                                                                                                                                               [10, 20]
                                                                                                                                                                                                               False
                                                       This
               if name == 'n':
                                                                          B. If <filter exp> evaluates to a true value, then add
                                                    function
                                                                                                                                                                               >>> nums = { 'I': 1.0, 'V': 5, 'X': 10}
                                                                                the value of <map exp> to the result list
                      return n
                                                   represents
                                                                                                                                                                               >>> nums['X']
               elif name == 'd':
                                                   a rational
                                                                       The result of calling repr on a value is
                                                     number
                      return d
                                                                                                                                                                               >>> nums['I'] = 1
                                                                       what Python prints in an interactive session
                                                                                                                                                                               >>> nums['L'] = 50
        return select
                                                                       The result of calling str on a value is
                                                                                                                                                                               >>> nums
def numer(x):
                                                                       what Python prints using the print function
                                                                                                                                                                               {'X': 10, 'L': 50, 'V': 5, 'I': 1}
                                       Constructor is a
       return x('n')
                                                                                                                                                                               >>> sum(nums.values())
                                   higher-order function
                                                                          >>> 12e12
                                                                                                                >>> print(today)
def denom(x):
                                                                                                                                                                               66
                                                                          120000000000000.0
                                                                                                                2014-10-13
                                                                                                                                                                               >>> dict([(3, 9), (4, 16), (5, 25)])
      return x('d')
                                                                          >>> print(repr(12e12))
                                      Selector calls x
                                                                                                                                                                               {3: 9, 4: 16, 5: 25}
>>> nums.get('A', 0)
                                                                          1200000000000000.0
Lists:
                                                                        str and repr are both polymorphic; they apply to any object
                                                                                                                                                                               0
>>> digits = [1, 8, 2, 8]
                                                                                                                                                                               >>> nums.get('V', 0)
                                                                        repr invokes a zero-argument method __repr__ on its argument
>>> len(digits)
                                                                        >>> today.__repr__()
'datetime.date(2014, 10, 13)'
                                                                                                                          >>> today.__str__()
                                                                                                                                                                               >>> {x: x*x for x in range(3,6)}
                        digits__
>>> digits[3]
                                                                                                                                                                               {3: 9, 4: 16, 5: 25}
                                                  8
                                                        2
                                                              8
                                            1
                                                                        Memoization:
                                                                                                                                   def memo(f):
                                                                                                                                                                               >>> suits = ['coin', 'string', 'myriad']
>>> [2, 7] + digits * 2
                                                                                                                                          cache = {}
                                                                                                fib(5)
                                                                                                                                                                               >>> suits.pop()————
                                                                                                                                                                                                                         Remove and return
[2, 7, 1, 8, 2, 8, 1, 8, 2, 8]
                                                                                                                                          def memoized(n):
                                                                                                                                                                               'myriad'
>>> suits.remove('string')
                                                                                                                                                                                myriad
                                                                                                                                                                                                                        the last element
>>> pairs = [[10, 20], [30, 40]]
                                                                                                                                                if n not in cache:
                                                                                                                                                                                                                          Remove a value
                                                                                                                      fib(4)
                                                                              fib(3) or
                                                                                                                                                                               >>> suits.append('cup')
                                                                                                                                                      cache[n] = f(n)
>>> pairs[1]
                        pairs
[30, 40]
                                                                                                                                                return cache[n]
                                                                                                                                                                               >>> suits.extend(['sword', 'club'])
                                                       10
                                                             20
                                                                       fib(1)
                                                                                    fib(2)
                                                                                                                                        return memoized
 >>> pairs[1][0]
                                                                                                                                                                               >>> suits[2] = 'spade'
                                                                                                                                                                                                                                       Add all
                                                                                                                                                                               >>> suits
['coin', 'cup', 'spade', 'club']
                                                                                                           fib(2) o
                                                                                                                                fib(3)
30
                                                                                                                                                                                                                                       values
                                                                              fib(0)
                                                                                          fib(1)
                                                                                                                                                                                                                                  Replace a
Executing a for statement:
                                                                                                                                                                               >>> suits[0:2] = ['diamond'] -
                                                                                                     fib(0)
                                                                                                                 fib(1)
                                                                                                                          fib(1)
                                                                                                                                        fib(2)
 for <name> in <expression>:
                                                                                                                                                                               >>> suits
['diamond', 'spade', 'club']
>>> suits.insert(0, 'heart')
Add an element
at an index
                                                       30
                                                           40
       <suite>
                                                                                                                                  fib(0)
                                                                                                                                              fib(1)
                                                                       Call to fib
 1. Evaluate the header <expression>
                                                                          Found in cache
                                                                                                                                                                                                                           at an index
                                                                                                                                                                               >>> suits
    which must yield an iterable value (a sequence)
                                                                       O Skipped
                                                                                                                                                                               ['heart', 'diamond', 'spade', 'club']
                                                                      Type dispatching: Look up a cross-type implementation of an
 2. For each element in that sequence,
                                                                                                                                                                               Identity:
                                                                      operation based on the types of its arguments

Type coercion: Look up a function for converting one type to
     in order:
                                                                                                                                                                               <exp0> is <exp1>
   A. Bind <name> to that element in
                                                                                                                                                                               evaluates to True if both <exn0> and
                                                                      another, then apply a type-specific implementation.
        the current frame
                                                                                                                                                                               <exp1> evaluate to the same object
   B. Execute the <suite>
                                                                                            \Theta(b^n) Exponential growth. Recursive fib takes
                                                                          e are positive I {\bf k_2} such that \leq k_2 \cdot f(n) than some {\bf m}
                                                                                                                                                                               Equality:
<exp0> == <exp1>
                                                                                                         \Theta(\phi^n) steps, where \phi=\frac{1+\sqrt{5}}{2}\approx 1.61828 Incrementing the
 Unpacking in a
                                    A sequence of
                                                                                                                                                                               evaluates to True if both <exp0> and
  for statement:
                            fixed-length sequences
                                                                                                         Incrementing the problem scales R(n)
                                                                                                                                                                               <exp1> evaluate to equal values
                                                                                                        by a factor
                                                                                                                                                                               Identical objects are always equal values
>>> pairs=[[1, 2], [2, 2], [3, 2], [4, 4]]
                                                                                            \Theta(n^2)
                                                                                                        Quadratic growth. E.g., overlap
 >>> same count = 0
                                                                                                                                                                               You can copy a list by calling the list
                                                                          there \mathbf{k_1} and \mathbf{k_2} R(n):
                                                                                                         Incrementing n increases R(n) by the
                                                                                                                                                                               constructor or slicing the list from the
                                                                      f(n)
          A name for each element in a
                                                                                                        problem size n
                                                                                                                                                                               beginning to the end.
              fixed-length sequence
                                                                                             \Theta(n)
                                                                                                        Linear growth. E.g., factors or exp
>>> for (x, y) in pairs:
 if x == y:
                                                                                 VΙ
                                                                                                                                                                               Constants: Constant terms do not affect
                                                                      R(n) = \Theta(f)
means that
constants k_1 \cdot f(n) \le k_1 \cdot f
                                                                                                                                                                               the order of growth of a process
                                                                                        \Theta(\log n)
                                                                                                        Logarithmic growth. E.g., exp_fast
                                                                                                                                                                               \Theta(n) \Theta(500 \cdot n) \Theta(\frac{1}{500} \cdot n) Logarithms: The base of a logarithm does
                                                                                                                                                                                                \Theta(500 \cdot n)
                   same_count = same_count + 1
                                                                                                        Doubling the problem only increments R(n)
 >>> same_count
                                                                                              \Theta(1) Constant. The problem size doesn't matter
                                                                                                                                                                               not affect the order of growth of a process
                                                                                                                                                                                \Theta(\log_2 n) \quad \  \Theta(\log_{10} n)
                                                                                                                                                                                                                      \Theta(\ln n)
      ..., -3, -2, -1, 0, 1, 2, 3, 4, ...
                                                                       Global frame
                                                                                                                       -> func make withdraw(balance) [parent=Global]
                                                                                                                                                                               Nesting: When an inner process is repeated
                                                                                           make_withdraw
                                                                                                                                                                               for each step in an outer process, multiply
                                                                                                                         >func withdraw(amount) [parent=f1]
                                                                                                                                                                               the steps in the outer and inner processes
                                                                                                  withdraw
                                                                                                                        >>> withdraw = make_withdraw(100)
                                                                                                                                                                               to find the total number of steps
                    range(-2, 2)
                                                                                                                        >>> withdraw(25)
                                                                                                                                                                               def overlap(a, b):
                                                                       f1: make withdraw [parent=Global]
                                                                                                                                                                                      for item in a: Outer: length of a
 Length: ending value - starting value
                                                                                                  balance 50
                                                                                                                        >>> withdraw(25)
 Element selection: starting value + index
                                                                           The parent
                                                                                                 withdraw
                                                                                                                                                                                           if item in b:

count += 1 Inner: length of b
                                                                        frame contains
                                                                                                                       50
                                                                                                                       def make_withdraw(balance):
                                                                                                   Return
                                                                        the balance of
  >>> list(range(-2, 2)) \langle List constructor
                                                                                                    value
                                                                                                                            def withdraw(amount):
                                                                             withdraw
                                                                                                                                                                                      return count
  [-2, -1, 0, 1]
                                                                                                                                    nonlocal balance
                                                                                                                                                                               If a and b are both length n,
                                                                       f2: withdraw [parent=f1]
                                                                                                                                    if amount > balance:
    return 'No funds
 >>> list(range(4)) { Range with a 0 starting value
                                                                                                                                                                               then overlap takes \Theta(n^2) steps
                                                                                                  amount 25
                                                                                                                                                                               Lower-order terms: The fastest-growing part
                                                                           Every call
  [0, 1, 2, 3]
                                                                                                                                    balance = balance - amount
                                                                                                   Return
value 75
                                                                                                                                                                               of the computation dominates the total
                                                                         decreases the
                                                                                                                                    return balance
Membership:
                                         Slicing:
                                                                         same balance
                                                                                                                                                                               \Theta(n^2) \quad \Theta(n^2 + n) \quad \Theta(n^2 + 500 \cdot n + \log_2 n + 1000)
                                                                                                                              return withdraw
>>> digits = [1, 8, 2, 8]
                                         >>> digits[0:2]
                                                                       f3: withdraw [parent=f1]
>>> 2 in digits
                                         [1, 8]
                                                                                                                         •No nonlocal statement
                                                                                                                            Status
                                                                                                                                                                        Effect
                                         >>> digits[1:]
                                                                                                 amount 25
                                                                                                                                                                     Create a new binding from name "x" to number 2
>>> 1828 not in digits
                                         [8, 2, 8]
                                                                                                                         •"x" is not bound locally
                                                                                                                                                                     in the first frame of the current environment
                                                                                                   Return
value 50
True
                                                                                                                                                                     Re-bind name "x" to object 2 in the first frame
                                         Slicing creates
                                                                                                                         •No nonlocal statement
                                                                        Strings as sequences:
                                                                                                                         •"x" is bound locally
                                            a new object
                                                                                                                                                                     of the current environment
                                                                       >>> city = 'Berkeley'
                                                                                                                         •nonlocal x
                                                                        >>> len(city)
                                                                                                                                                                     Re-bind "x" to 2 in the first non-local frame of
Functions that aggregate iterable arguments
                                                                                                                         •"x" is bound in a
                                                                                                                                                                     the current environment in which "x" is bound
                                                                        8
•sum(iterable[, start]) -> value
                                                                                                                           non-local frame
                                                                        >>> city[3]
•max(iterable[, key=func]) -> value
                                                                                                                         •nonlocal x
 max(a, b, c, ...[, key=func]) -> value
                                                                                                                         •"x" is not bound in
                                                                                                                                                                     SyntaxError: no binding for nonlocal 'x' found
                                                                       >>> 'here' in "Where's Waldo?'
 min(iterable[, key=func]) -> value
                                                                                                                           a non-local frame
                                                                       True
 min(a, b, c, ...[, key=func]) -> value
                                                                                                                         •nonlocal x
                                                                       >>> 234 in [1, 2, 3, 4, 5]
•all(iterable) -> bool
any(iterable) -> bool
                                                                                                                         •"x" is bound in a
                                                                                                                                                                     SyntaxError: name 'x' is parameter and nonlocal
```

non-local frame

•"x" also bound locally

>>> [2, 3, 4] in [1, 2, 3, 4]

False

def right(self):

return self.branches[1]

```
Python object system:
                                                                       Nodes
                                                         •Path
  Recursive description:
                                                                                      Idea: All bank accounts have a balance and an account holder;
                                       Root value -
                                                    √3 ₹
  •A tree has a root value
                                                                                       the Account class should add those attributes to each of its instances
                                                                             Values
  and a list of branches
                                    Branch —
  • Each branch is a tree
                                                                                                                  >>> a = Account('Jim')
                                                                                         A new instance is
  •A tree with zero branches is called a leaf
                                                                                                                   >>> a.holder
                                                                                       created by calling a
                                             1
                                                                                                                   'Jim'
                                                                                                class
                                                                                                                   >>> a.balance
  Relative description:
                                                                                                                                              An account instance
                                        0
                                                  1
                                                         1
  •Each location is a node
                                                                                      When a class is called:
                                                                                                                                                       holder: 'Jim'
                                                                                                                                        balance: 0
  •Each node has a value
•One node can be the
                                                                                     1.A new instance of that class is created:
                                       Leaf 🥕
                                                              0
                                                                                              _init__ method of the class is called with the new object as its first
   parent/child of another
                                                                                        argument (named self), along with any additional arguments provided in the
  def tree(root, branches=[]):
                                                                                        call expression.
                                          Verifies the
       for branch in branches:
                                                                                                              class Account:
                                       tree definition
                                                                                                                       __init__(self, account_holder):
self.balance = 0
           assert is_tree(branch)
                                                                                                                 >def
                                                                                          init is called a
       return [root] + list(branches)
                                                                                            constructor
                                                                                                                       self.holder = account_holder
  def root(tree):
                                                                                                                       deposit(self, amount):
                           Creates a list from a
       return tree[0]
                                                                                                                       _self.balance = self.balance + amount return self.balance
                           sequence of branches
  def branches(tree):
                                                                  3
                                                                                        self should always be
                                                                                                                       withdraw(self, amount):
if amount > self.balance:
    return 'Insufficient funds'
                          Verifies that tree is
                                                                                                                   def
                                                                                       bound to an instance of
       return tree[1:]
                              bound to a list
                                                                                       the Account class or a subclass of Account
  def is_tree(tree):
                                                                                                                       self.balance = self.balance - amount
       if (type(tree) != list)or len(tree) < 1:</pre>
                                                                                                                       return self.balance
           return False
                                                                                1
       for branch in branches(tree):
                                                                                                               >>> type(Account.deposit)
                                             >>> tree(3, [tree(1),
                                                                                        Function call: all
           if not is_tree(branch):
                                                                                                               >>> type(a.deposit)
                                                            tree(2, [tree(1),
                                                                                        arguments within
                                             . . .
                return False
                                             [3, [1], [2, [1], [1]]] tree(1)])])
                                                                                           parentheses
                                                                                                               <class 'method'
       return True
  def is_leaf(tree):
                                                                                                                >>> Account.deposit(a, 5)
                                                                                        Method invokation:
       return not branches(tree)
                                    def fib_tree(n):
   if n == 0 or n == 1:
                                                                                        One object before the dot and other
   def leaves(tree):
                                                                                                                   a.deposit(2)
                                                                                                                                              Call expression
       """The leaf values in tree.
>>> leaves(fib_tree(5))
                                              return tree(n)
                                                                                         arguments within
                                                                                                               12
                                          else:
                                                                                            parentheses
       [1, 0, 1, 0, 1, 1, 0, 1]
                                                                                                                     Dot expression
                                              left = fib\_tree(n-2)
                                              right = fib_tree(n-1)
fib_n = root(left) + root(right)
return tree(fib_n, [left, right])
       if is_leaf(tree):
                                                                                                                    <expression> . <name>
           return [root(tree)]
       else:
                                                                                       The <expression> can be any valid Python expression.
           return sum([leaves(b) for b in branches(tree)], [])
                                                                                       The <name> must be a simple name.
                                                                                       Evaluates to the value of the attribute looked up by <name> in the object
        Tree:
  class
                                                                                       that is the value of the <expression>.
      def __init__(self, root, branches=[]):
                                                         Built-in isinstance
                                                                                       To evaluate a dot expression:

1. Evaluate the <expression> to the left of the dot, which yields
           self.root = root
                                                      function: returns True if
           for branch in branches:
                                                      branch has a class that
                                                                                            the object of the dot expression
           assert (isinstance(branch, Tree) <
self.branches = list(branches)</pre>
                                                      is or inherits from Tree
                                                                                            <name> is matched against the instance attributes of that object;
                                                                                           if an attribute with that name exists, its value is returned If not, <name> is looked up in the class, which yields a class
                                          def fib_tree(n):
      def is leaf(self):
           return not self.branches
                                              if \overline{n} == 0 or n == 1:
                                                                                            attribute value
                                                  return Tree(n)
                                                                                            That value is returned unless it is a function, in which case a
                                              else:
  def leaves(tree):
                                                                                            bound method is returned instead
                                                   left = fib_Tree(n-2)
       'The leaf values in Tree instance
                                                   right = fib\_Tree(n-1)
     if tree.is_leaf():
                                                                                       Assignment statements with a dot expression on their left-hand side affect
                                                   fib_n = left.root+right.root
                                                                                       attributes for the object of that dot expression
          return [tree.root]
                                                   return Tree(fib_n,[left, right])
      else:
                                                                                        • If the object is an instance, then assignment sets an instance attribute
          return sum([leaves(b) for b in tree.branches], [])
                                                                                        • If the object is a class, then assignment sets a class attribute
 class Link:
                                                     Link(4. Link(5))
                       Some zero
                                                                                                  Account class
                                                                                                                       interest: 0.02 0.04 0.05 (withdraw, deposit, __init
     empty = (() < length sequence
                                                     Link instance
                                                                       Link instance
                                                                                                    attributes
          __init__(self, first, rest=empty):
self.first = first
                                                      first:
                                                                       first:
                                                                                                             balance:
                                                                                                                                                      balance:
                                                                                                                        0
'Jim'
                                                                                                                                     Instance
          self.rest = rest
                                                                                                                                                      holder:
                                                                                                            holder:
                                                                                         attributes of
                                                                                                                                  attributes of
                                                       rest:
                                                                        rest:
           _getitem__(self, i):
                                                                                                            interest: 0.08
                                                                                          jim_account
                                                                                                                                   tom account
          if i == 0:
                                                                                                                                     >>> jim_account.interest = 0.08
              return self.first
                                                                                       >>> iim account = Account('Jim')
                                         Sequence abstraction special names:
          else:
                                                                                            tom_account = Account('Tom')
                                                                                                                                     >>> jim_account.interest
              return self.rest[i-1]
                                                                                                                                     0.08
                                                                                       >>> tom_account.interest
                                           _getitem__ Element selection []
            len (self):
                                                                                                                                     >>> tom_account.interest
                                                                                       0.02
          return 1 + len(self.rest)
                                                                                                                                     0.04
                                                                                       >>> jim_account.interest
                                                        Built-in len function
                                           len_
           _repr__(self):
                                                                                                                                     >>> Account.interest = 0.05
                                                                                       0.02
                                                                                                                                     >>> tom_account.interest
          if self.rest:
                                                                                       >>> Account.interest = 0.04
              rest_str = ', ' + repr(self.rest)
                                                                                                                                     0.05
                                                                                       >>> tom_account.interest
                                                                  Contents of the
                                                                                                                                     >>> jim_account.interest
          else:
              rest_str = 🛄
                                                                  repr string of
                                                                                                                                     0.08
                                                                                       >>> jim_account.interest
          return 'Link({0}{1})'.format(self.first, rest_str)
                                                                 a Link instance
                                                                                       0.04
def extend_link(s, t):
                                         >>> s = Link(3, Link(4))
                                                                                       class CheckingAccount(Account):
    """A bank account that charges for withdrawals."""
     if s is Link.empty:
                                         >>> extend_link(s, s)
Link(3, Link(4, Link(3, Link(4))))
          return t
                                                                                            withdraw_fee = 1
     else:
                                                                                            interest = 0.01
         return Link(s.first, extend_link(s.rest, t))
                                                                                                withdraw(self,
                                                                                                                 amount):
Python built-in sets:
                              >>> 3 in s
                                               >>> s.union({1, 5})
{1, 2, 3, 4, 5}
                                                                                               return Account.withdraw(self, amount + self.withdraw_fee)
>>> s = {3, 2, 1, 4, 4}
                              True
>>> s
                                                   s.intersection({6, 5, 4, 3})
                              >>> len(s)
                                                                                                return (super(), withdraw(
                                                                                                                                  amount + self.withdraw fee)
\{1, 2, 3, 4\}
                                               \{3, 4\}
A binary search tree is a binary tree where each root is larger than all values in its left branch and smaller than all values in its right branch
                                                                                       To look up a name in a class:
                                                                                       1. If it names an attribute in the class, return the attribute value.
class BTree(Tree):
                                                                                       2. Otherwise, look up the name in the base class, if there is one.
     empty = Tree(None)
                                                                                       >>> ch = CheckingAccount('Tom') # Calls Account.__init_
         __init__(self, root, left=empty, right=empty):
Tree.__init__(self, root, [left, right])
     def
                                                                                       >>> ch_interest
                                                                                                              # Found in CheckingAccount
                                                                                       0.01
     @property
     def left(self):
                                                                                       >>> ch.deposit(20) # Found in Account
                                                                                       20
         return self.branches[0]
                                                                                        >>> ch.withdraw(5) # Found in CheckingAccount
     @property
```

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'Tom'