COMPUTER SCIENCE 61A

October 13, 2016

1 Linked Lists

1.1 Implementation

```
class Link:
    empty = ()
    def __init__(self, first, rest=empty):
        assert rest is Link.empty or isinstance (rest, Link)
        self.first = first
        self.rest = rest
    def ___getitem___(self, i):
        if i == 0:
            return self.first
        return self.rest[i-1]
    def ___len___(self):
        return 1 + len(self.rest)
    def __repr__(self):
        if self.rest is Link.empty:
            return 'Link({})'.format(self.first)
        else:
            return 'Link({}, {})'.format(self.first,
                                          repr(self.rest))
```

1.2 Questions

1. Write a function remove_duplicates that takes as input a sorted linked list of integers, lnk, and mutates lnk so that all duplicates are removed.

```
def remove_duplicates(lnk):
    """

>>> lnk = Link(1, Link(1, Link(1, Link(1, Link(5)))))
>>> unique = remove_duplicates(lnk)
>>> len(unique)
2
>>> len(lnk)
2
"""
```

2. Define reverse, which takes in a linked list and reverses the order of the links. The function may *not* return a new list; it must mutate the original list. Return a pointer to the head of the reversed list.

```
def reverse(lnk):
    """
    >>> a = Link(1, Link(2, Link(3)))
    >>> r = reverse(a)
    >>> r.first
    3
    >>> r.rest.first
    2
    """
```

3. Write multiply_lnks, which takes in a Python list of Link objects and multiplies them element-wise. It should return a new linked list. If not all of the Link objects are of equal length, return a linked list whose length is that of the shortest linked list given. You may assume the Link objects are shallow linked lists, and that lst_of_lnks contains at least one linked list.

```
def multiply_lnks(lst_of_lnks):
    """

    >>> a = Link(2, Link(3, Link(5)))
    >>> b = Link(6, Link(4, Link(2)))
    >>> c = Link(4, Link(1, Link(0, Link(2))))
    >>> p = multiply_lnks([a, b, c])
    >>> p.first
    48
    >>> p.rest.first
    12
    >>> p.rest.rest.rest
    ()
    """
```

2 Midterm Review

1. Define a function foo that takes in a list lst and returns a new list that keeps only the even-indexed elements of lst and multiplies each of those elements by the corresponding index.

```
def foo(lst):
    """
    >>> x = [1, 2, 3, 4, 5, 6]
    >>> foo(x)
    [0, 6, 20]
    """
return [
```

2. Implement the functions max_product, which takes in a list and returns the maximum product that can be formed using nonconsecutive elements of the list. The input list will contain only numbers greater than or equal to 1.

```
def max_product(lst):
    """Return the maximum product that can be formed using lst
    without using any consecutive numbers
    >>> max_product([10,3,1,9,2]) # 10 * 9
    90
    >>> max_product([5,10,5,10,5]) # 5 * 5 * 5
    125
    >>> max_product([])
    1
    """
```

3. An **expression tree** is a tree that contains a function for each non-leaf root, which can be either '+' or '*'. All leaves are numbers. Implement eval_tree, which evaluates an expression tree to its value. You may want to use the functions sum and prod, which take a list of numbers and compute the sum and product respectively.

```
def eval_tree(tree):
    """Evaluates an expression tree with functions as root
    >>> eval_tree(tree(1))
    1
    >>> expr = tree('*', [tree(2), tree(3)])
    >>> eval_tree(expr)
    6
    >>> eval_tree(tree('+', [expr, tree(4), tree(5)]))
    15
    """
```

4. The **quicksort** sorting algorithm is an efficient and commonly used algorithm to order the elements of a list. We choose one element of the list to be the **pivot** element and partition the remaining elements into two lists: one of elements less than the pivot and one of elements greater than the pivot. We recursively sort the two lists, which gives us a sorted list of all the elements less than the pivot and all the elements greater than the pivot, which we can then combine with the pivot for a completely sorted list.

First, implement the quicksort_list function. Choose the first element of the list as the pivot. You may assume that all elements are distinct.

5. We can also use quicksort to sort linked lists! Implement the quicksort_link function, without constructing additional Link instances.

You can assume that the <code>extend_links</code> function is already defined. It takes two linked lists and mutates the first so that the ending node points to the second. <code>extend_link</code> returns the head of the first linked list.

```
>>> 11, 12 = Link(1, Link(2)), Link(3, Link(4))
>>> 13 = extend_links(11, 12)
>>> 13
Link(1, Link(2, Link(3, Link(4))))
>>> 11 is 13
True
```

	quicksort_link(link):
	>>> s = Link(3, Link(1, Link(4))) >>> quicksort_link(s)
]	Link(1, Link(3, Link(4)))
:	if
	return link
I	pivot, =
	less, greater =
7	while link is not Link.empty:
	<pre>curr, rest = link, link.rest</pre>
	if
	else:
	link =
	less =
(greater =

6. Implement widest_level, which takes a Tree instance and returns the elements at the depth with the most elements.

```
def widest level(t):
      11 11 11
     >>> sum([[1], [2]], [])
      [1, 2]
     >>> t = Tree(3, [Tree(1, [Tree(1), Tree(5)]),
                      Tree (4, [Tree (9, [Tree (2)])])])
     >>> widest_level(t)
      [1, 5, 9]
      11 11 11
     levels = []
     x = [t]
             = sum( , [])
     return max(levels, key=____)
7. Complete redundant_map, which takes a tree t and a function f, and applies f to
 the node (2^d) times, where d is the depth of the node. The root has a depth of 0.
 def redundant_map(t, f):
   11 11 11
   >>> double = lambda x: x * 2
   >>> tree = Tree(1, [Tree(1), Tree(2, [Tree(1, [Tree(1)])])])
   >>> print_levels(redundant_map(tree, double))
    [2] \# 1 \star 2 \hat{} (1) ; Apply double one time
    [4, 8] # 1 * 2 ^ (2), 2 * 2 ^ (2); Apply double two times
    [16] \# 1 \times 2 ^ (2 ^ 2) ; Apply double four times
    [256] \# 1 \star 2 ^ (2 ^ 3); Apply double eight times
   new_f =
```

t.branches = _____

return t